

Package ‘ReMFPCA’

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Type Package

Title Regularized Multivariate Functional Principal Component Analysis

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Description Methods and tools for implementing regularized multivariate functional principal component analysis ('ReMFPCA') for multivariate functional data whose variables might be observed over different dimensional domains. 'ReMFPCA' is an object-oriented interface leveraging the extensibility and scalability of R6. It employs a parameter vector to control the smoothness of each functional variable. By incorporating smoothness constraints as penalty terms within a regularized optimization framework, 'ReMFPCA' generates smooth multivariate functional principal components, offering a concise and interpretable representation of the data. For detailed information on the methods and techniques used in 'ReMFPCA', please refer to Haghbin et al. (2023) <doi:10.48550/arXiv.2306.13980>.

URL <https://github.com/haghbinh/ReMFPCA>

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*.mfd *Scalar multiplication of an 'mfd' object*

Description

Scalar multiplication of an 'mfd' object. One object must be an 'mfd', and the other one a scalar

Usage

```
## S3 method for class 'mfd'
obj1 * obj2
```

Arguments

obj1 An 'mfd' object or an scalar
obj2 An 'mfd' object or an scalar

Value

An 'mfd' object

See Also[basismfd, mfd](#)

.mvmfdMultiplication of an 'mvmfd' object with a scalar*

Description

Multiplication of an 'mvmfd' object with a scalar

Usage

```
## S3 method for class 'mvmfd'  
obj1 * obj2
```

Arguments

obj1 An 'mvmfd' object or a scalar
obj2 An 'mvmfd' object or a scalar

Value

An 'mvmfd' object

See Also[mvmfd, mvbasismfd](#)

+.mfd*Add two 'mfd' objects*

Description

Add two 'mfd' objects

Usage

```
## S3 method for class 'mfd'  
obj1 + obj2 = NULL
```

Arguments

obj1 An 'mfd' object
obj2 An 'mfd' object or a scalar

Value

The sum of the two 'mfd' objects

See Also

[basismfd,mfd](#)

<code>+.mvmfd</code>	<i>Addition of two 'mvmfd' objects</i>
----------------------	--

Description

Addition of two 'mvmfd' objects

Usage

```
## S3 method for class 'mvmfd'  
obj1 + obj2 = NULL
```

Arguments

<code>obj1</code>	An 'mvmfd' object
<code>obj2</code>	An optional 'mvmfd' object

Value

An 'mvmfd' object

See Also

[mvmfd,mvbasismfd](#)

<code>-.mfd</code>	<i>Subtract two 'mfd' objects</i>
--------------------	-----------------------------------

Description

Subtract two 'mfd' objects

Usage

```
## S3 method for class 'mfd'  
obj1 - obj2 = NULL
```

Arguments

`obj1` An 'mfd' object
`obj2` An 'mfd' object or a scalar

Value

The difference between the two 'mfd' objects

See Also

[basismfd, mfd](#)

<code>-.mvmfd</code>	<i>Subtraction of two 'mvmfd' objects</i>
----------------------	---

Description

Subtraction of two 'mvmfd' objects

Usage

```
## S3 method for class 'mvmfd'  
obj1 - obj2 = NULL
```

Arguments

`obj1` An 'mvmfd' object
`obj2` An optional 'mvmfd' object

Value

An 'mvmfd' object

See Also

[mvmfd, mvbasismfd](#)

 basismfd

Define a Set of Multidimensional Functional Basis

Description

The ‘basismfd’ class represents a set of multidimensional basis functions. This class utilizes basis objects from the ‘fda’ package, such as B-splines and Fourier bases.

Constructor for ‘basismfd’ objects (same as `Basismfd(...)`)

Usage

```
Basismfd(...)
```

```
Basismfd(...)
```

Arguments

... A list of ‘basisfd’ objects

Active bindings

`basis` A list of basis objects from the ‘fda’ package.

`dimSupp` The dimension of the support domain of the ‘basismfd’ object.

`supp` The matrix representing the ranges of the dimensions.

`gram` The Gram matrix.

`nbasis` A numeric vector containing the number of bases.

Methods

Public methods:

- [basismfd\\$new\(\)](#)
- [basismfd\\$eval\(\)](#)
- [basismfd\\$print\(\)](#)
- [basismfd\\$clone\(\)](#)

Method `new()`: The constructor function for objects of the class ‘basismfd’ (same as `Basismfd(...)`)

Usage:

```
basismfd$new(...)
```

Arguments:

... A list of ‘basisfd’ objects

Method `eval()`: Evaluate the ‘basismfd’ object at given argument values

Usage:

```
basismfd$eval(evalarg)
```

Arguments:

evalarg A list of numeric vectors of argument values at which the 'basismfd' is to be evaluated

Returns: A list of evaluated values

Method print(): Print method for 'basismfd' objects

Usage:

```
basismfd$print(...)
```

Arguments:

... Additional arguments to be passed to 'print' Getter and setter for 'basis' field Getter and setter for 'dimSupp' field Getter and setter for 'nbasis' field Getter and setter for 'supp' field Getter and setter for 'gram' field

Method clone(): The objects of this class are cloneable with this method.

Usage:

```
basismfd$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

Examples

```
require(fda)
bs1 <- create.fourier.basis(c(0, 2 * pi), 5)
bs2 <- create.bspline.basis(c(0, 1), 7)
bs3 <- create.exponential.basis(c(0, 2), 3)
# 1-D Basis ##### (similar to the fd features)
mdbs1 <- Basismfd(bs1)
mdbs1$basis
mdbs1$dimSupp
mdbs1$nbasis
mdbs1$supp
mdbs1$gram
mdbs1$eval(1:7 / 10)
image(as.matrix(mdb1$gram))

##### 2-D Basis ##### (fd cannot handle this)
mdbs2 <- Basismfd(bs1, bs2)
mdbs2$basis
mdbs2$dimSupp
mdbs2$nbasis
mdbs2$supp
dim(mdb2$gram)
arg_mdbs <- list(1:10, 1:9 / 10)
mdbs2$eval(arg_mdbs)
image(as.matrix(mdb2$gram))
```

bimfdplot *Bivariate plot for 'mvmfd' objects*

Description

Bivariate plot for 'mvmfd' objects

Usage

```
bimfdplot(mvmfd_obj, type = "l", lty = 1, xlab = "", ylab = "", main = "", ...)
```

Arguments

mvmfd_obj	An 'mvmfd' object
type	Type of plot ('l' for lines, 'p' for points, etc.)
lty	Line type
xlab	Label for the x-axis
ylab	Label for the y-axis
main	Main title
...	Additional arguments for the matplot function

See Also

[mvmfd](#), [mvbasismfd](#)

inprod_mfd *Compute the inner product between two objects of class 'mfd'*

Description

Compute the inner product between two objects of class 'mfd'

Usage

```
inprod_mfd(mfd_obj1, mfd_obj2)
```

Arguments

mfd_obj1	An 'mfd' object
mfd_obj2	An 'mfd' object

Value

The inner products matrix between the two 'mfd' objects

See Also[basismfd, mfd](#)

inprod_mvmd	<i>Compute the inner product between two objects of class 'mvmd'</i>
-------------	--

Description

Compute the inner product between two objects of class 'mvmd'

Usage

```
inprod_mvmd(mvmd_obj1, mvmd_obj2)
```

Arguments

mvmd_obj1	An 'mvmd' object
mvmd_obj2	An 'mvmd' object

Value

The inner products matrix between the two 'mvmd' objects

See Also[mvmd, mvbasismfd](#)

is.basismfd	<i>Check if an object is of class 'basismfd'</i>
-------------	--

Description

Check if an object is of class 'basismfd'

Usage

```
is.basismfd(fobj)
```

Arguments

fobj	The object to check.
------	----------------------

Value

TRUE if the object is of class 'basismfd', FALSE otherwise.

See Also[is.mvbasismfd, is.mfd, is.mvmd](#)

is.mfd	<i>Check if an object is of class 'mfd'</i>
--------	---

Description

Check if an object is of class 'mfd'

Usage

```
is.mfd(fobj)
```

Arguments

fobj The object to check.

Value

TRUE if the object is of class 'mfd', FALSE otherwise.

See Also

[is.mvbasismfd](#), [is.basismfd](#), [is.mvmfd](#)

is.mvbasismfd	<i>Check if an object is of class 'mvbasismfd'</i>
---------------	--

Description

Check if an object is of class 'mvbasismfd'

Usage

```
is.mvbasismfd(fobj)
```

Arguments

fobj The object to check.

Value

TRUE if the object is of class 'mvbasismfd', FALSE otherwise.

See Also

[is.basismfd](#), [is.mfd](#), [is.mvmfd](#)

is.mvmfd	<i>Check if an object is of class 'mvmfd'</i>
----------	---

Description

Check if an object is of class 'mvmfd'

Usage

```
is.mvmfd(fdoobj)
```

Arguments

fdoobj The object to check.

Value

TRUE if the object is of class 'mvmfd', FALSE otherwise.

See Also

[is.mvbasismfd](#), [is.mfd](#), [is.basismfd](#)

length	<i>Length of an object of classes 'mfd' or 'mvmfd'.</i>
--------	---

Description

Length of an object of an object of classes 'mfd' or 'mvmfd'.

Usage

```
length(x, ...)
```

Arguments

x An object of classes 'mfd' or 'mvmfd'.
... all 'length' function arguments.

mean	<i>mean of an object of classes 'mfd' or 'mvmfd'.</i>
------	---

Description

mean of an object of classes 'mfd' or 'mvmfd'.

Usage

```
mean(x, ...)
```

Arguments

x	An object of classes 'mfd' or 'mvmfd'.
...	all 'mean' function arguments.

Value

An object of class 'mfd'

mfd	<i>Define a Set of Multidimensional Functional Data objects</i>
-----	---

Description

The 'mfd' class represents a set of multidimensional functional data with 'basismfd' object. Functional data objects are constructed by specifying a set of basis functions and a set of coefficients defining a linear combination of these basis functions.

Constructor for 'mfd' objects (same as Mfd(...))

Usage

```
Mfd(argval = NULL, X, mdbs, method = "data")
```

Arguments

argval	A list of numeric vectors of argument values at which the 'mfd' object is to be evaluated
X	A numeric matrix corresponds to basis expansion coefficients if 'method="coefs"' and discrete observations if 'method="data"'.
mdbs	a basismfd object
method	determine the 'X' matrix type as "coefs" and "data".

Active bindings

`basis` an object of the class 'basismfd'.

`coefs` a matrix of the coefficients.

`nobs` number of the observation

Methods**Public methods:**

- `mfd$new()`
- `mfd$eval()`
- `mfd$print()`
- `mfd$clone()`

Method `new()`: Constructor for 'mfd' objects (same as `Mfd(...)`)

Usage:

```
mfd$new(argval = NULL, X, mdbs, method = "data")
```

Arguments:

`argval` A list of numeric vectors of argument values at which the 'mfd' object is to be evaluated

`X` A numeric matrix corresponds to basis expansion coefficients if 'method="coefs"' and discrete observations if 'method="data"'.

`mdbs` a basismfd object

`method` determine the 'X' matrix type as "coefs" and "data".

Method `eval()`: Evaluation an 'mfd' object in some arguments.

Usage:

```
mfd$eval(evalarg)
```

Arguments:

`evalarg` a list of numeric vector of argument values at which the mfd is to be evaluated.

Returns: A matrix of evaluated values

Method `print()`: Print method for 'mfd' objects

Usage:

```
mfd$print(...)
```

Arguments:

... Additional arguments to be passed to 'print'

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
mfd$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

See Also[basismfd](#)**Examples**

```

require(fda)
bs1 <- create.fourier.basis(c(0,2*pi),5)
bs2 <- create.bspline.basis(c(0,1),7)
bs3 <- create.exponential.basis(c(0,2),3)

#1-D mfd :_____
argval <- seq(0,2*pi,length.out=100)
nobs <- 10;
X <- outer(sin(argval),seq(0.5,1.5,length.out=nobs))
mdbs1 <- Basismfd(bs1)
mfd1 <- Mfd(X=X, mdbs = mdbs1)
inprod_mfd(mfd1,mfd1)
norm_mfd(mfd1)
mfd0 <- 2.5*mfd1
mfd1-mfd0
mfd1[1:3]

mfd1$eval(argval)
mfd1c <- Mfd(X=mfd1$coefs, mdbs = mdbs1, method = "coefs")
all.equal(c(mfd1$basis,mfd1$coefs,mfd1$nobs),c(mfd1c$basis,mfd1c$coefs,mfd1c$nobs))
length(mfd1)
mean(mfd1)
plot(mfd1)

```

mvbasismfd

*Define a Set of Multivariate Multidimensional Functional Basis***Description**

The ‘mvbasismfd’ a set of multivariate multidimensional basis functions. This class utilizes basis objects ‘basismfd’.

Constructor for ‘mvbasismfd’ objects (same as ‘Mvbasismfd’)

Usage

```
Mvbasismfd(basis)
```

```
Mvbasismfd(basis)
```

```
## S3 method for class 'mvbasismfd'
mvbasismfd_obj[i = "index"]
```

Arguments

basis	A list of basisfd objects
mvbasismfd_obj	An 'mvmfd' object
i	An index or indices specifying the subsets to extract for the first dimension

Value

An 'mvbasismfd' object containing the specified subsets

Active bindings

nvar	number of variables
basis	A list of 'mvbasisfd' objects
dimSupp	A sequence of positive integers specifying support domain of the 'mvbasismfd' object.
nbasis	A list of integers specifying the number of basis functions
supp	A list of matrices specifying the support of basis functions
gram	The Gram matrix.

Methods**Public methods:**

- [mvbasismfd\\$new\(\)](#)
- [mvbasismfd\\$eval\(\)](#)
- [mvbasismfd\\$clone\(\)](#)

Method `new()`: Constructor for 'mvbasismfd' objects (same as `Mvbasismfd(...)`)

Usage:

```
mvbasismfd$new(basis)
```

Arguments:

basis A list of 'basismfd' objects

Method `eval()`: Evaluate the 'mvbasismfd' object at given argument values

Usage:

```
mvbasismfd$eval(evalarg)
```

Arguments:

evalarg A list of numeric vectors of argument values at which the 'mvbasismfd' is to be evaluated

Returns: A list of evaluated values

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
mvbasismfd$clone(deep = FALSE)
```

Arguments:

deep Whether to make a deep clone.

See Also

[mvmfd](#), [basismfd](#)

mvmfd

Define a Set of Multivariate Multidimensional Functional Data objects

Description

The ‘mvmfd’ class represents functional data ...

Constructor for ‘mvmfd’ objects (same as ‘Mvmfd’)

Usage

```
Mvmfd(...)
```

Arguments

... A ‘mfd’ objects which have separated by comma

Active bindings

basis A ‘mvbasismfd’ object

coefs a matrix of the coefficients.

nobs number of observation

nvar number of variables

Methods**Public methods:**

- [mvmfd\\$new\(\)](#)
- [mvmfd\\$eval\(\)](#)
- [mvmfd\\$print\(\)](#)
- [mvmfd\\$clone\(\)](#)

Method `new()`: Constructor for ‘mvmfd’ objects (same as ‘Mvmfd’)

Usage:

```
mvmfd$new(...)
```

Arguments:

... A ‘mfd’ objects which have separated by comma

Method `eval()`: Eval method for ‘mvmfd’ objects

Usage:

```
mvmfd$eval(evalarg)
```

Arguments:

`evalarg` A list of numeric vectors of argument values at which the ‘mvmfd’ is to be evaluated.

Returns: A list of evaluated values

Method `print()`: Print method for ‘mvmfd’ objects

Usage:

```
mvmfd$print(...)
```

Arguments:

... Additional arguments to be passed to ‘print’

Method `clone()`: The objects of this class are cloneable with this method.

Usage:

```
mvmfd$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

See Also

[mvbasmfd](#), [mfd](#)

Examples

```
require(fda)
bs1 <- create.fourier.basis(c(0, 2 * pi), 5)
bs2 <- create.bspline.basis(c(0, 1), 7)
bs3 <- create.exponential.basis(c(0, 2), 3)
nobs <- 10
argval1 <- seq(0, 2 * pi, length.out = 12)
X1 <- outer(sin(argval1), seq(0.5, 1.5, length.out = nobs))
mdbs1 <- Basismfd(bs1)
mfd1 <- Mfd(argval1, X1, mdbs1)
mdbs2 <- Basismfd(bs1)
argval2 <- argval1
X2 <- outer(cos(argval2), seq(0.2, 1.5, length.out = nobs))
mfd2 <- Mfd(argval2, X2, mdbs1)
mvmfd1 <- Mvmfd(mfd1, mfd2)
mvmfd1[1]
mvmfd1[1, 1]
mvmfd1[1:5, 2]
mvmfd1[, 1]
mvmfd1[1:5, ]
evalarg <- list(argval1, argval2)
mvmfd1$eval(evalarg)
mvmfd1 + mvmfd1
mean(mvmfd1)
inprod_mvmfd(mvmfd1, mvmfd1)
norm_mvmfd(mvmfd1)
plot(mvmfd1)
bimfdplot(mvmfd1)
```

norm_mfd	<i>Compute the norm of an object of class 'mfd'</i>
----------	---

Description

Compute the norm of an object of class 'mfd'

Usage

```
norm_mfd(mfd_obj)
```

Arguments

mfd_obj An object of class 'mfd'

Value

The norm vector of the an object of class 'mfd'

See Also

[basismfd](#), [mfd](#)

norm_mvmd	<i>Compute the norm of an object of class 'mvmd'</i>
-----------	--

Description

Compute the norm of an object of class 'mvmd'

Usage

```
norm_mvmd(mvmd_obj)
```

Arguments

mvmd_obj An 'mvmd' object

Value

The norm vector of the an object of class 'mvmd'

See Also

[mvmd](#), [mvbasismfd](#)

pen_fun	<i>Penalty Function</i>
---------	-------------------------

Description

Calculate the penalty matrix for ‘mvmfd’ objects.

Usage

```
pen_fun(data, devorder = 2, type)
```

Arguments

data	an object of class ‘mvmfd’.
devorder	The order of the derivative.
type	The type of penalty. The types "coefpen" and "basispen" is supported.

Value

The penalty matrix.

plot	<i>plots an object of classes ‘mfd’, ‘mvmfd’ or ‘remfpca’</i>
------	---

Description

plot an object of classes ‘mfd’, ‘mvmfd’ or ‘remfpca’

Usage

```
plot(x, ...)
```

Arguments

x	An object of classes ‘mfd’, ‘mvmfd’ or ‘remfpca’
...	all ‘plot’ function arguments.

remfpca

A Class for 'ReMFPCA' objects

Description

The 'remfpca' class represents regularized functional principal components components.

The 'remfpca' class represents regularized functional principal components ('ReMFPCs') components.

Usage

```
Remfpca(
  mvmfd_obj,
  ncomp,
  alpha = NULL,
  centerfns = TRUE,
  alpha_orth = TRUE,
  penalty_type = "coefpen"
)
```

Arguments

mvmfd_obj	An 'mvmfd' object representing the multivariate functional data.
ncomp	The number of functional principal components to retain.
alpha	A list or vector specifying the regularization parameter(s) for each variable. If NULL, the regularization parameter is estimated internally.
centerfns	Logical indicating whether to center the functional data before analysis.
alpha_orth	Logical indicating whether to perform orthogonalization of the regularization parameters.
penalty_type	The type of penalty to be applied on the coefficients. The types "coefpen" and "basispen" is supported. Default is "coefpen".

Active bindings

pc_mfd an object of class 'mvmfd' where the first indices (fields) represents harmonics and second indices represents variables

lsv = Left singular values vectors

values = the set of eigenvalues

alpha = The vector of penalties parameters

GCVs = generalized cross validations

mean_mfd a multivariate functional data object giving the mean function

Methods**Public methods:**

- [remfpca\\$new\(\)](#)
- [remfpca\\$clone\(\)](#)

Method new():*Usage:*

```
remfpca$new(
  mvmfd_obj,
  ncomp,
  alpha = NULL,
  centerfns = TRUE,
  alpha_orth = TRUE,
  penalty_type = "coefpen"
)
```

Arguments:

`mvmfd_obj` An 'mvmfd' object representing the multivariate functional data.

`ncomp` The number of functional principal components to retain.

`alpha` A list or vector specifying the regularization parameter(s) for each variable. If NULL, the regularization parameter is estimated internally.

`centerfns` Logical indicating whether to center the functional data before analysis.

`alpha_orth` Logical indicating whether to perform orthogonalization of the regularization parameters.

`penalty_type` The type of penalty to be applied on the coefficients. The types "coefpen" and "basispen" is supported. Default is "coefpen".

Method clone(): The objects of this class are cloneable with this method.

Usage:

```
remfpca$clone(deep = FALSE)
```

Arguments:

`deep` Whether to make a deep clone.

See Also

[mvmfd](#)

Examples

```
require(fda)
# Brownian Bridge simulation on [0,1]
M <- 110 # number of components
N <- 20 # number of instances
n <- 100 # number of grides
t0 <- seq(0, 1, len = n)
j <- 1:M
alpha1 <- list(a1 = 2^seq(0, 1, length.out = 3), a2 = 2^seq(0, 1, length.out = 3))
```

```

psi_1 <- function(t, m) sin(m * pi * t) # eigenfunction of BB
psi_2 <- function(t, m) sin((2 * m - 1) * pi / 2 * t) # eigenfunction of BM
PC_1 <- outer(t0, j, FUN = psi_1) # n by M matrix
PC_2 <- outer(t0, j, FUN = psi_2) # n by M matrix
Z <- matrix(rnorm(N * M), nr = M)
lambda <- matrix(2 / (pi * (2 * j - 1)), nr = M, nc = N)
X_1t <- PC_1 %*% (lambda * Z)
X_2t <- PC_2 %*% (lambda * Z)
noise <- rnorm(n * N, 0, 0.1)
X_1 <- X_1t + noise
X_2 <- X_2t + noise
bs <- create.bspline.basis(c(0, 1), 51)
mdbs <- Basismfd(bs)
mfd1 <- Mfd(X = X_1, mdbs = mdbs)
mfd2 <- Mfd(X = X_2, mdbs = mdbs)
mvmfd_obj <- Mvmfd(mfd1, mfd2)
k <- 2
Re0 <- Remfpga(mvmfd_obj, ncomp = k, alpha = c(0, 0))
fpc0 <- Re0$pc_mfd
scores0 <- inprod_mvmfd(mvmfd_obj, fpc0)
dim(scores0)
Re0$alpha
Re1 <- Remfpga(mvmfd_obj, ncomp = k, alpha = alpha1)
Re1$alpha
Re3 <- Remfpga(mfd1, ncomp = k, alpha = alpha1$a1)
Re3$alpha

```

sd

Standard deviation of an object of class 'mfd'.

Description

Standard deviation an object of class 'mfd'.

Usage

```
sd(x, ...)
```

Arguments

x	An object of class 'mfd'
...	all 'sd' function arguments.

Value

An object of class 'mfd'

[.mfd *Extract subsets of an 'mfd' object*

Description

Extract subsets of an 'mfd' object

Usage

```
## S3 method for class 'mfd'  
mfd_obj[i = "index"]
```

Arguments

mfd_obj An 'mfd' object
i An index or indices specifying the subsets to extract

Value

An 'mfd' object containing the specified subsets

See Also

[basismfd](#), [mfd](#)

[.mvmfd *Extract subsets of an 'mvmfd' object*

Description

Extract subsets of an 'mvmfd' object

Usage

```
## S3 method for class 'mvmfd'  
mvmfd_obj[i = "index", j = "index"]
```

Arguments

mvmfd_obj An 'mvmfd' object
i An index or indices specifying the subsets to extract for the first dimension
j An index or indices specifying the subsets to extract for the second dimension

Value

An 'mvmfd' object containing the specified subsets

See Also[mvmfd,mvbasisbfd](#)

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